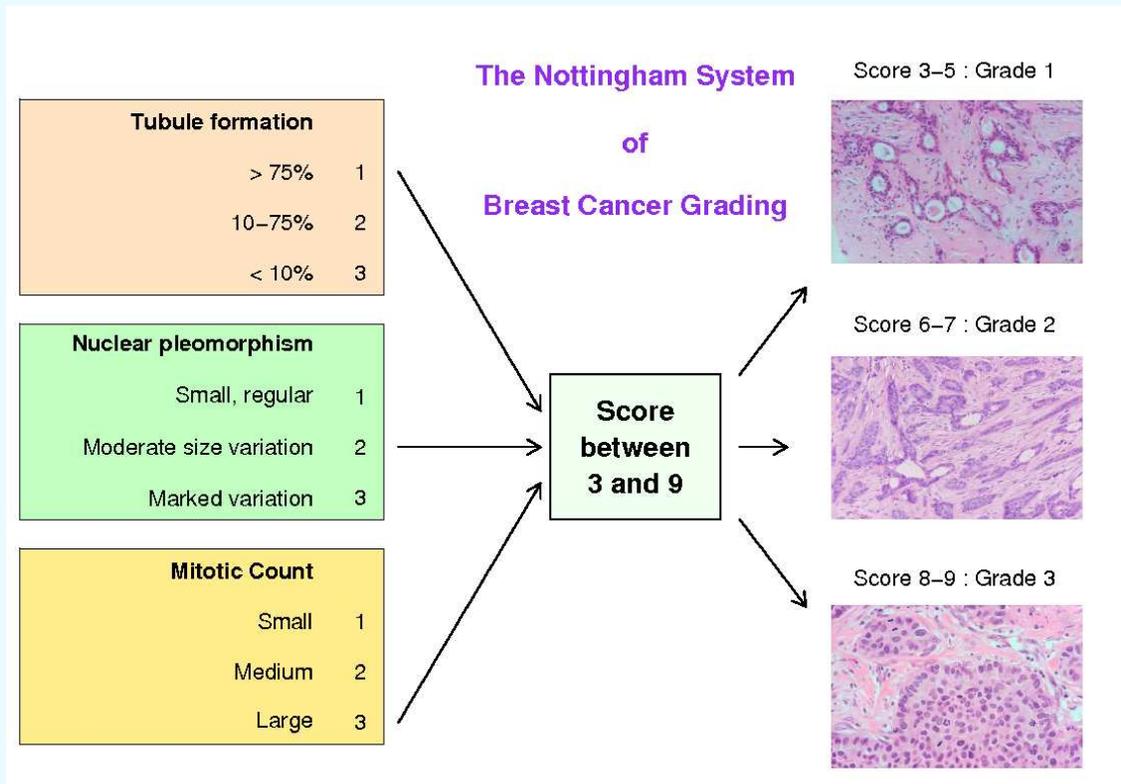


Assessing variability in histological grade of breast cancer tumours

T.R. Fanshawe, CHICAS, Department of Medicine, Lancaster University: t.fanshawe@lancaster.ac.uk

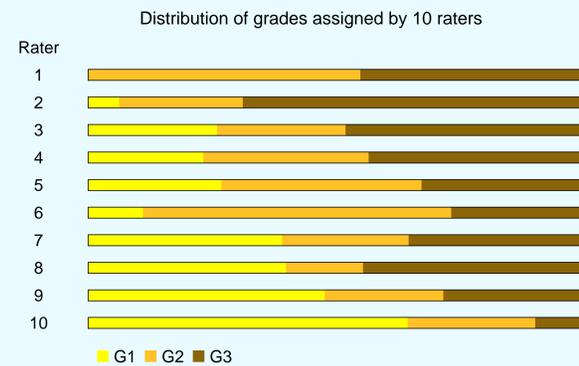


Data from the National External Quality Assurance (EQA) Scheme for Breast Cancer Histopathology:

- Digitised images of histological tissue sections of 52 breast cancer tumours
- 732 UK pathologists (raters) gave grades (G1, G2 or G3) to an average of 33 tumours each (63%)
- Each tumour was graded by between 390 (53%) and 513 (70%) raters
- No 'Ground Truth': grading is subjective

Are All Raters Equal?

- It seems not
- Big differences in distribution of grades awarded
- Rater 1 gave 0 Grade 1s out of 20 tumours
- Rater 10 gave 20 Grade 1s out of 31 tumours
- Different raters may have seen different tumours

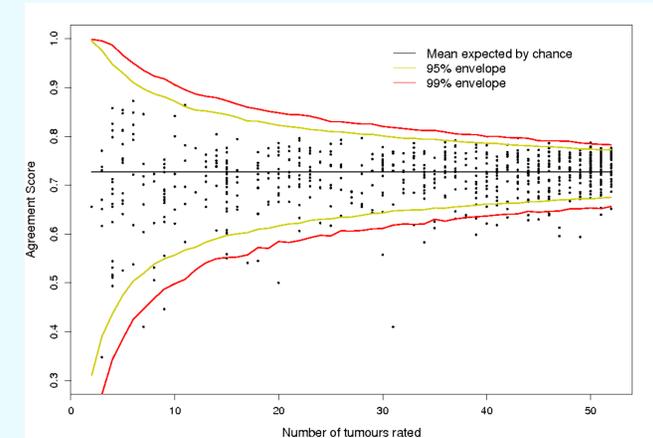


Acknowledgements

A.G. Lynch, I.O. Ellis, A.R. Green, R. Hanka
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 Fanshawe, Lynch *et al*: PLoS ONE 3(8): e2925. doi:10.1371/journal.pone.0002925

A Simple Summary Measure

- For each rater, calculate the proportion of raters with whom he agrees on a given tumour
- Average these across all tumours graded by the rater
- Plot values from all raters as a funnel plot (right)
- 95% and 99% envelopes estimated by Monte Carlo simulation
- Too many points outside envelopes: evidence that some raters are doing worse than others



Cumulative Logit Model : The Idea

- Each tumour has a 'true severity' μ on a hypothetical continuous scale
- There are also 'true' boundaries b_{12} and b_{23} on the scale that dictate the 'true' grade i.e. $\mu < b_{12} \Rightarrow G1$; $b_{12} < \mu < b_{23} \Rightarrow G2$; $\mu > b_{23} \Rightarrow G3$
- Each rater has his own set of boundary parameters that determine which grade he will assign (below right)

For rater j and tumour i :

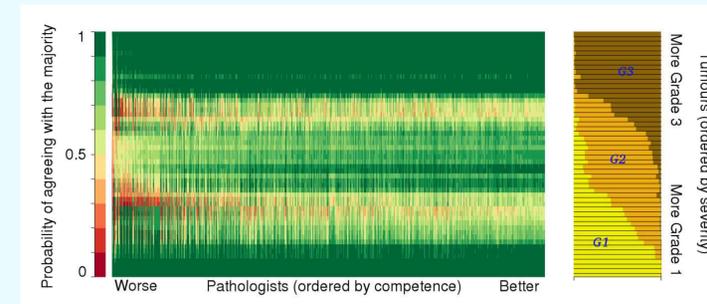
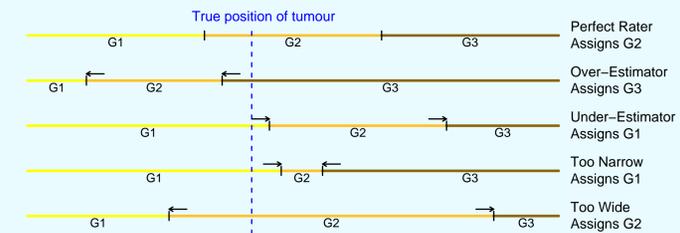
$$P(j \text{ assigns } G3 \text{ to } i) = \text{logit}^{-1}(f(i, j))$$

$$P(j \text{ assigns } G2 \text{ or } G3 \text{ to } i) = \text{logit}^{-1}(g(i, j))$$

$$f(i, j) = \lambda_i(\mu_i - b_{23,j})$$

$$g(i, j) = \lambda_i(\mu_i - b_{12,j})$$

(λ_i) are 'clarity' parameters, (μ_i) are 'severity' parameters
 ($b_{12,j}$) and ($b_{23,j}$) are 'boundary' parameters



- Why do raters disagree?
- Graph shows estimated boundaries b_{12} and b_{23} for each rater
- Most common discrepancy is for raters to either underestimate or over-estimate both boundaries

Results

- Sampling from posterior distributions enables quantities of interest to be estimated
- Heat-map shows the estimated probability, for each tumour, of a rater agreeing with the majority
- Right-hand panel shows the estimated marginal distribution of grades for each tumour

