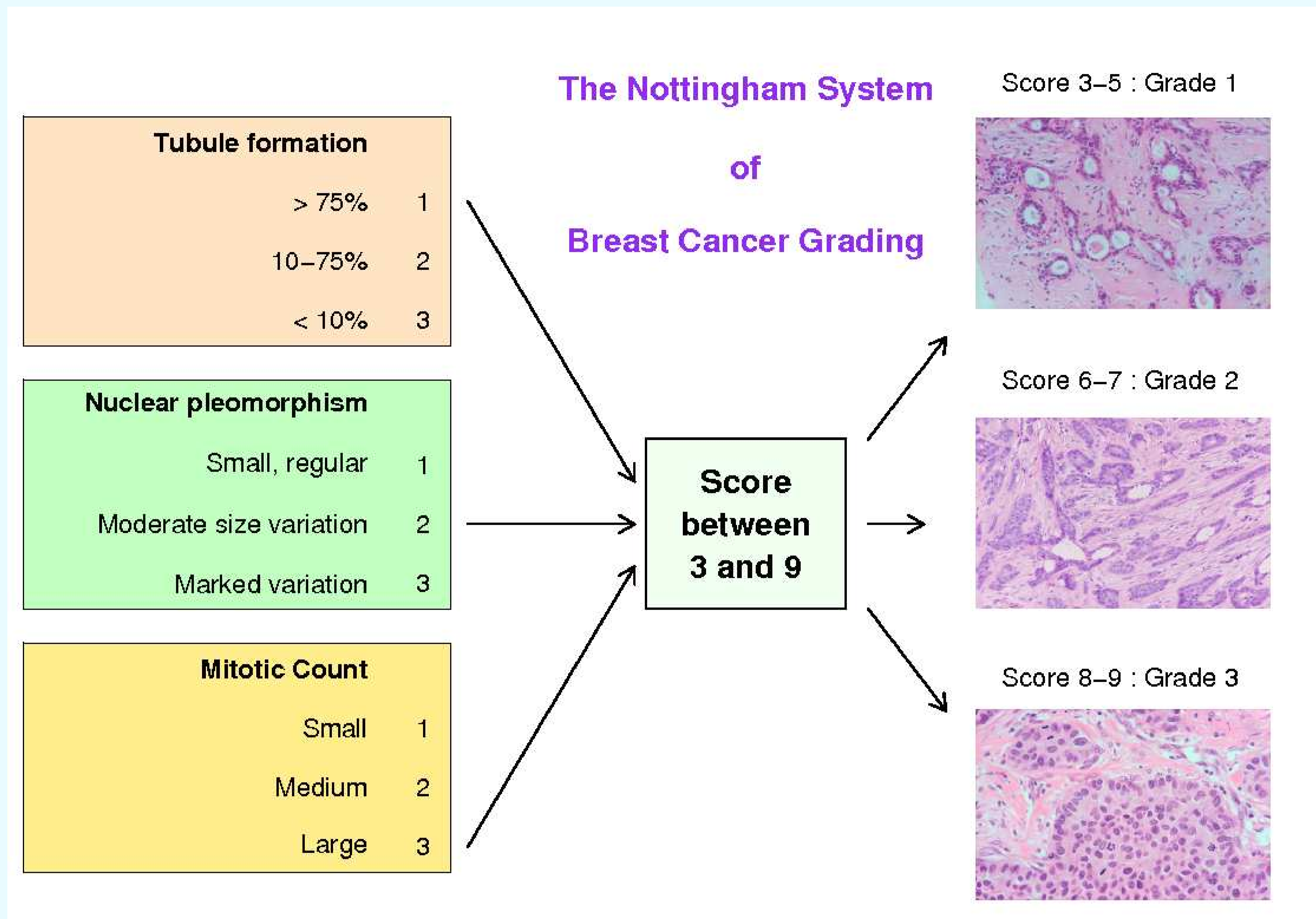


# Assessing variability in histological grade of breast cancer tumours

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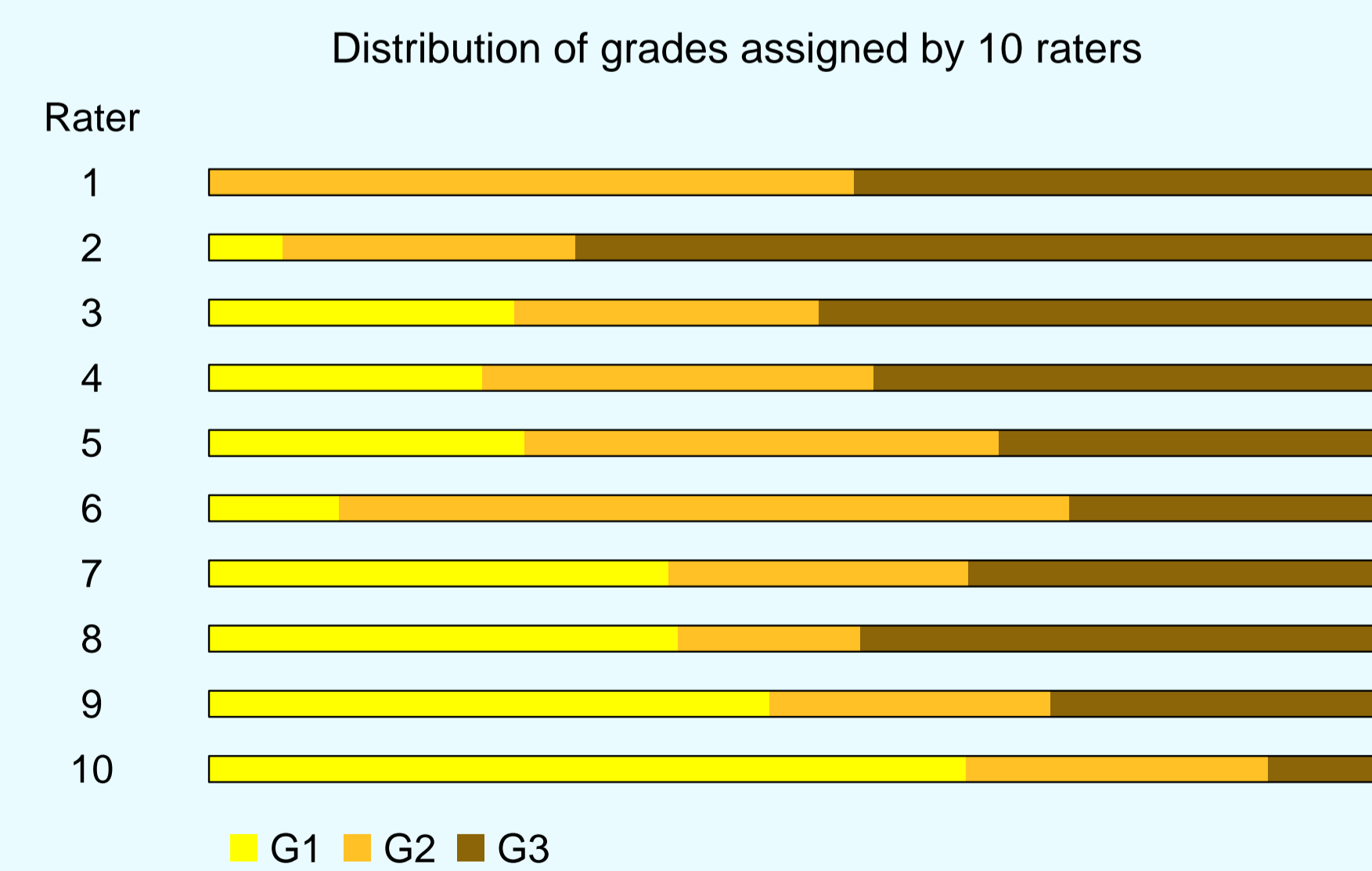


Data from the National External Quality Assurance (EQA) Scheme for Breast Cancer Histopathology:

- Digitised images of histological tissue sections of 52 breast cancer tumours
- 732 UK pathologists (raters) gave grades (G1, G2 or G3) to an average of 33 tumours each (63%)
- Each tumour was graded by between 390 (53%) and 513 (70%) raters
- No 'Ground Truth': grading is subjective

## Are All Raters Equal?

- It seems not
- Big differences in distribution of grades awarded
- Rater 1 gave 0 Grade 1s out of 20 tumours
- Rater 10 gave 20 Grade 1s out of 31 tumours
- Different raters may have seen different tumours

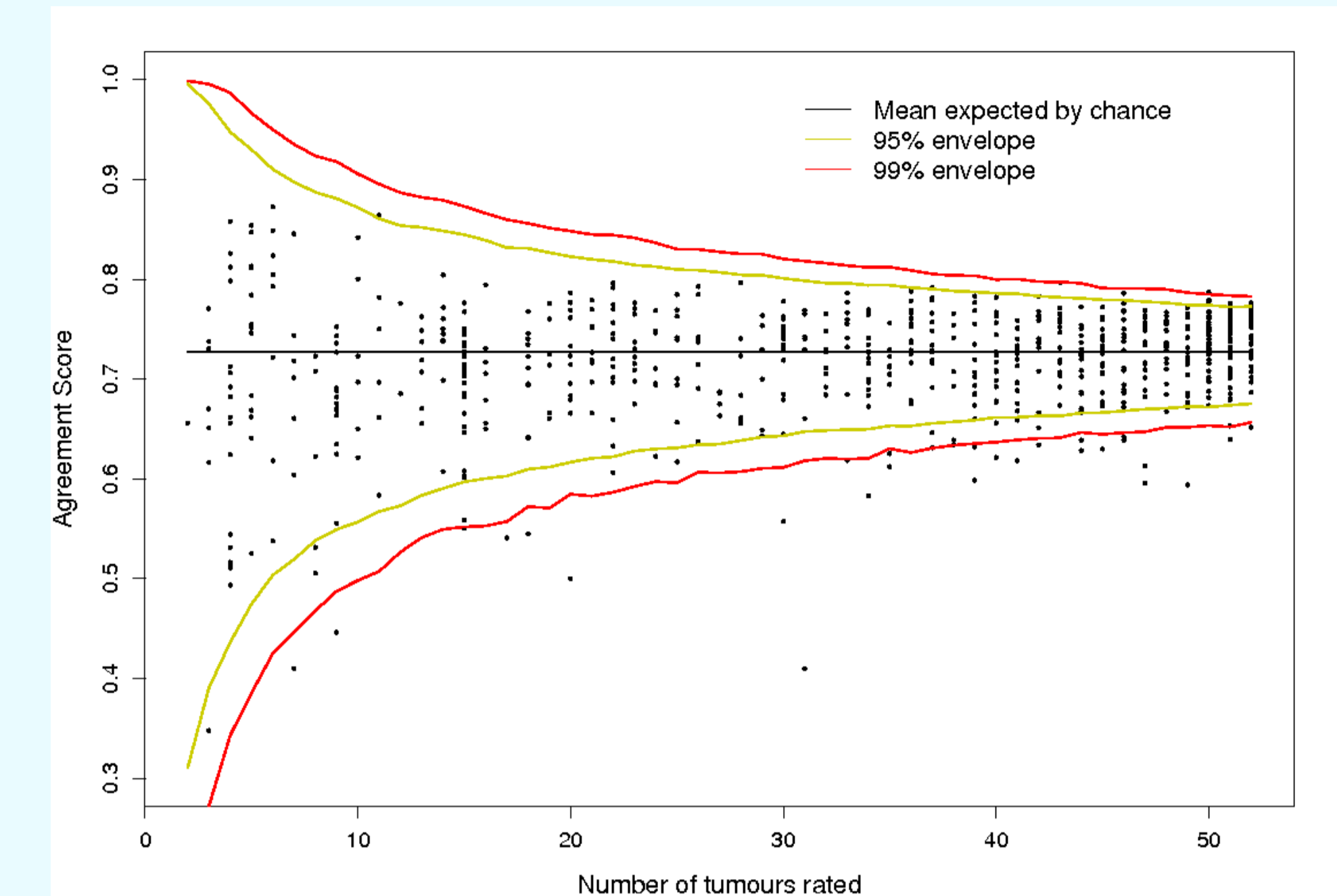


## Acknowledgements

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## A Simple Summary Measure

- For each rater, calculate the proportion of raters with whom he agrees on a given tumour
- Average these across all tumours graded by the rater
- Plot values from all raters as a funnel plot (right)
- 95% and 99% envelopes estimated by Monte Carlo simulation
- Too many points outside envelopes: evidence that some raters are doing worse than others



## Cumulative Logit Model : The Idea

- Each tumour has a 'true severity'  $\mu$  on a hypothetical continuous scale
- There are also 'true' boundaries  $b_{12}$  and  $b_{23}$  on the scale that dictate the 'true' grade i.e.  $\mu < b_{12} \Rightarrow G1$ ;  $b_{12} < \mu < b_{23} \Rightarrow G2$ ;  $\mu > b_{23} \Rightarrow G3$
- Each rater has his own set of boundary parameters that determine which grade he will assign (below right)

For rater  $j$  and tumour  $i$ :

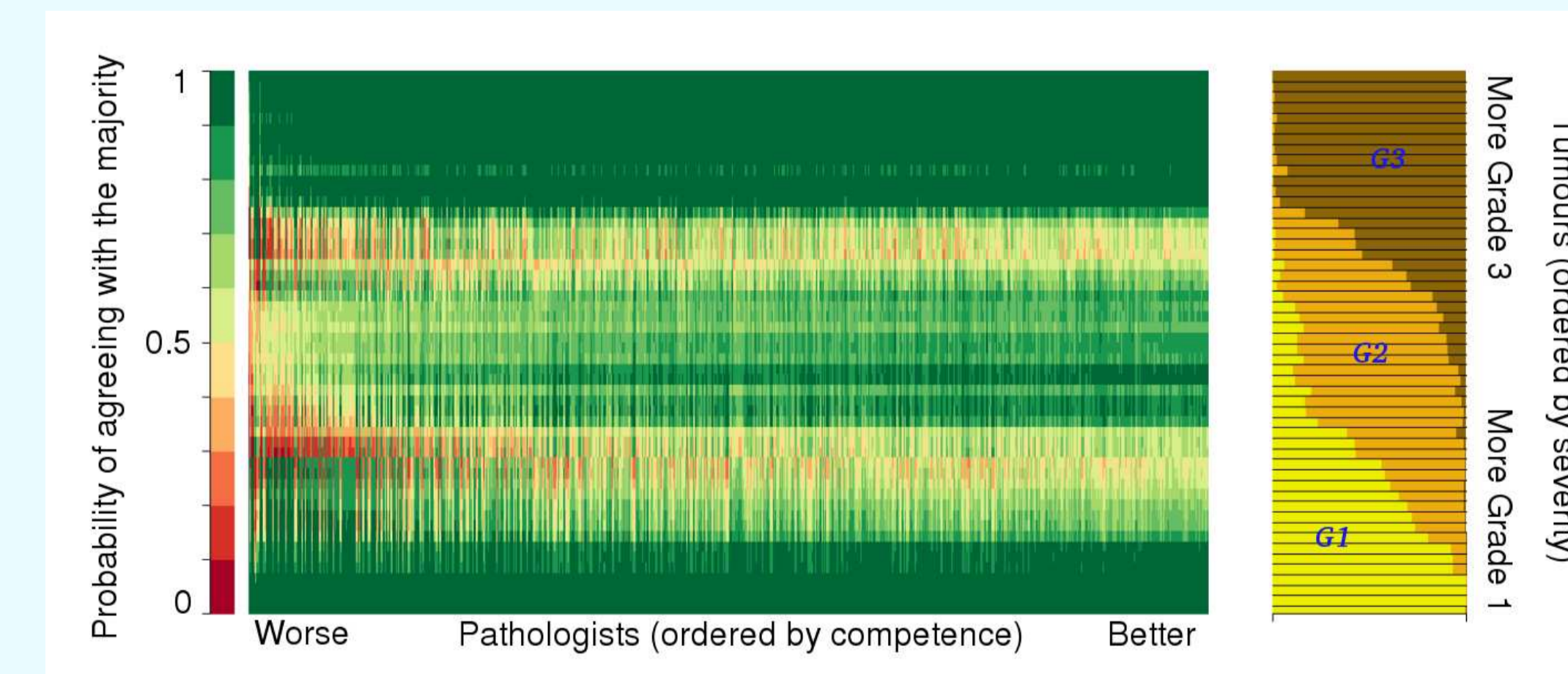
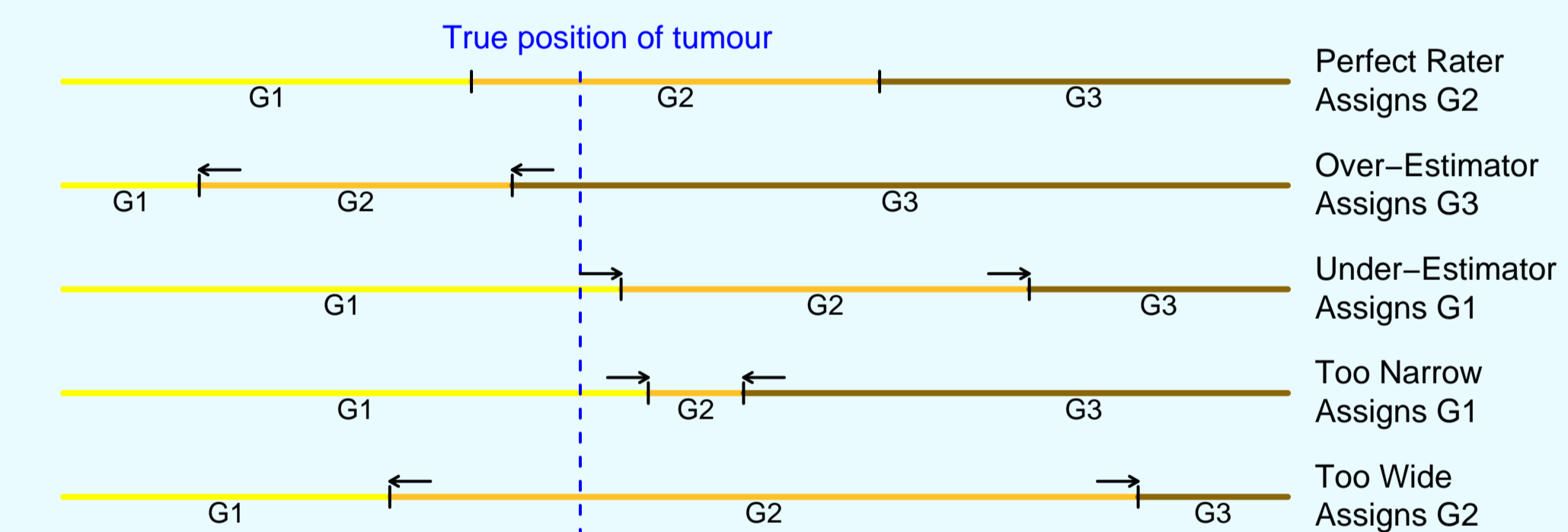
$$P(j \text{ assigns G3 to } i) = \text{logit}^{-1}(f(i, j))$$

$$P(j \text{ assigns G2 or G3 to } i) = \text{logit}^{-1}(g(i, j))$$

$$f(i, j) = \lambda_i(\mu_i - b_{23,j})$$

$$g(i, j) = \lambda_i(\mu_i - b_{12,j})$$

( $\lambda_i$ ) are 'clarity' parameters, ( $\mu_i$ ) are 'severity' parameters  
 ( $b_{12,j}$ ) and ( $b_{23,j}$ ) are 'boundary' parameters



- Why do raters disagree?
- Graph shows estimated boundaries  $b_{12}$  and  $b_{23}$  for each rater
- Most common discrepancy is for raters to either underestimate or over-estimate both boundaries

## Results

- Sampling from posterior distributions enables quantities of interest to be estimated
- Heat-map shows the estimated probability, for each tumour, of a rater agreeing with the majority
- Right-hand panel shows the estimated marginal distribution of grades for each tumour

